

Conditional statement

If  $\angle 1$  and  $\angle 2$  are vertical angles, then  $\angle 1 \cong \angle 2$ .

Contrapositive

If  $\angle 1$  is not congruent to  $\angle 2$ , then  $\angle 1$  and  $\angle 2$  are not vertical angles.

### 5-3 Indirect Proof

Indirect Proof

1. Assume conclusion is false
2. Reason until you contradict the given
3. State assumption is false

#### Example 1

Given: Mary received an A on the test.

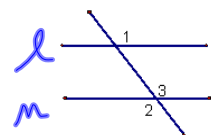
Prove: Her grade was  $\geq 90\%$ .

Assume Mary earned an 89.  
 If she earned an 89 she would have received a B.  
 ✗ Contradiction of given  
 Our assumption is false  
 Mary's grade was  $\geq 90\%$

#### Example 2

Given:  $\angle 1 \cong \angle 2$

Prove:  $\angle 1 \cong \angle 3$



Assume  $\angle 1 \not\cong \angle 3$   
 then  $l \parallel m$  b/c of corr  $\angle$ s  
 $\cong$ , then lines are  $\parallel$ .  
 If the lines are  $\parallel$ , then  $\angle 1 \cong \angle 2$   
 b/c alt ext  $\angle$ s are  $\cong$ .  
 ✗ Contradiction of given.  
 Our assumption is false  
 $\angle 1 \cong \angle 3$

Example 4

Given:  $\frac{1}{2y+4} = 20$

Prove:  $y \neq -2$

Assume  $y = -2$ .

$$\frac{1}{2(-2)+4} = 20 \rightarrow \frac{1}{0} = 20$$

Impossible & Contradicts given

Our assumption is false

$$y \neq -2$$

Homework

p. 258 #s 13-17, 19, 22  
not 15

5.3 before 5.2